

# Stochastic Geometry-based Trajectory Design for Multi-Purpose UAVs: Package and Data Delivery

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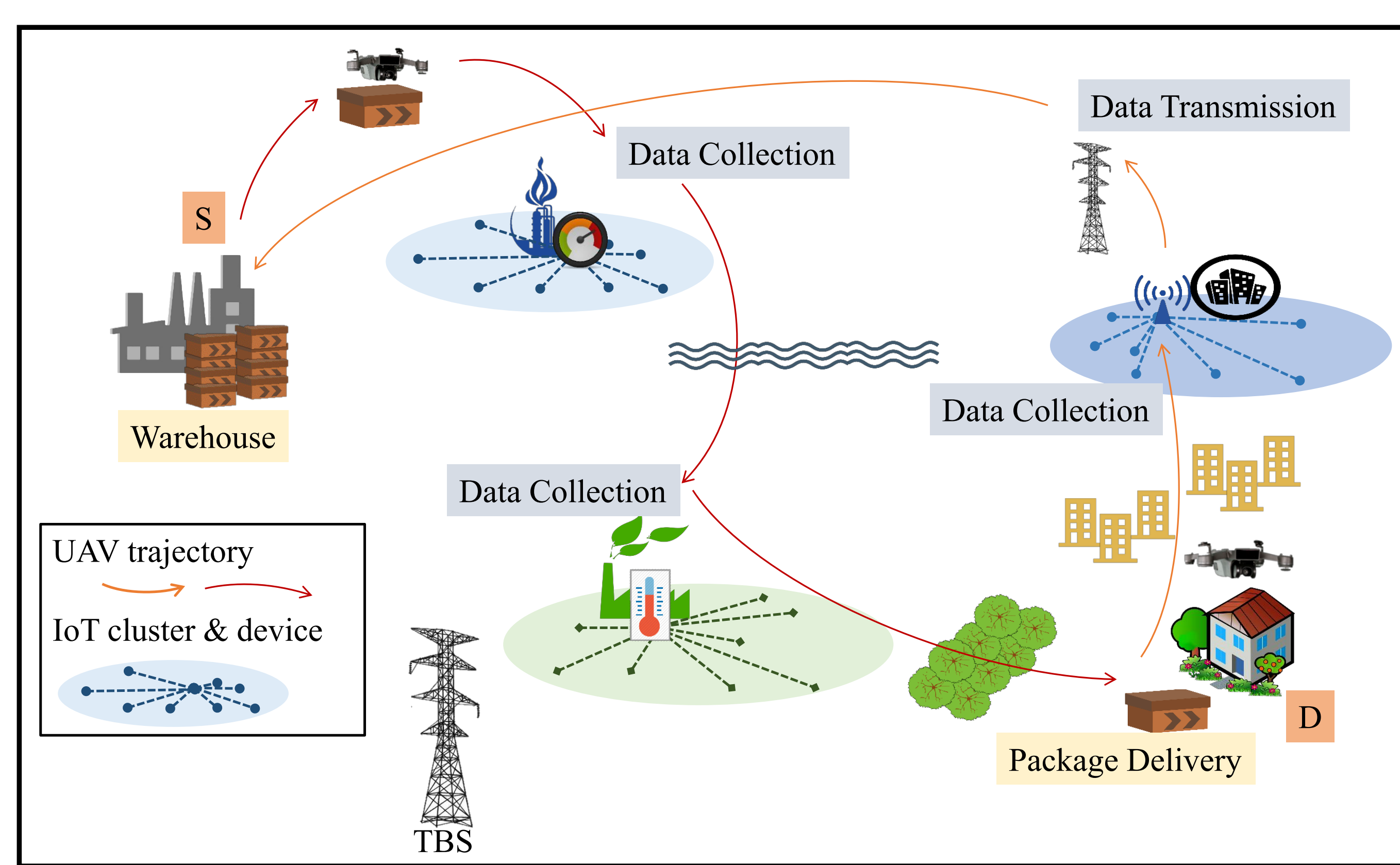
## Introduction

Challenges of future UAV-enabled networks:

- Limited aerial space and physical infrastructure.
- The traditional model of dedicated drones for a single function faces high cost and waste lots of energy.

Multi-purpose drones can be a solution: drones can be designed more flexibly to finish multiple tasks at the same time.

## System Model



- Locations of two types of IoT cluster centers and TBSs are modeled by three independent Poisson point processes (PPPs)  $\Phi_{i,1}$ ,  $\Phi_{i,2}$ ,  $\Phi_b$ .
- Locations of IoT devices are modeled by Matern cluster process (MCP).
- UAVs deliver the package from the warehouse (S) to destination (D), while collect data from IoT devices and forward the data to nearby TBSs.
- UAV's onboard battery is limited.

## IoT clusters & TBS Selection

- Order the IoT clusters/TBSs based on the distance and priority.
- UAVs consume all the energy to deliver the package and data.

## Communication Model

- The transmission time between UAVs and TBSs/ IoT devices are  $M/C_t$ ,  $M/C_i$ , where  $M$  is the data size and  $C_{\{\cdot\}}$  is the maximal achievable data rate.

## Trajectory Design

- Minimal time & maximum transmitted data path:

$$\mathcal{P}_1 : T_{total}^* | \Phi_{i,1}, \Phi_{i,2}, \Phi_b = \min_{\mathbf{h}, \mathbf{s}} T_{total},$$

$$s.t. \quad E_{total} \leq B_{max}, s_k \in \{0,1\}.$$

$$\mathcal{P}_2 : M_{total}^* | \Phi_{i,1}, \Phi_{i,2}, \Phi_b = \max_{\mathbf{h}, \mathbf{s}} M_{total},$$

$$s.t. \quad E_{total} \leq B_{max}, s_k \in \{0,1\}$$

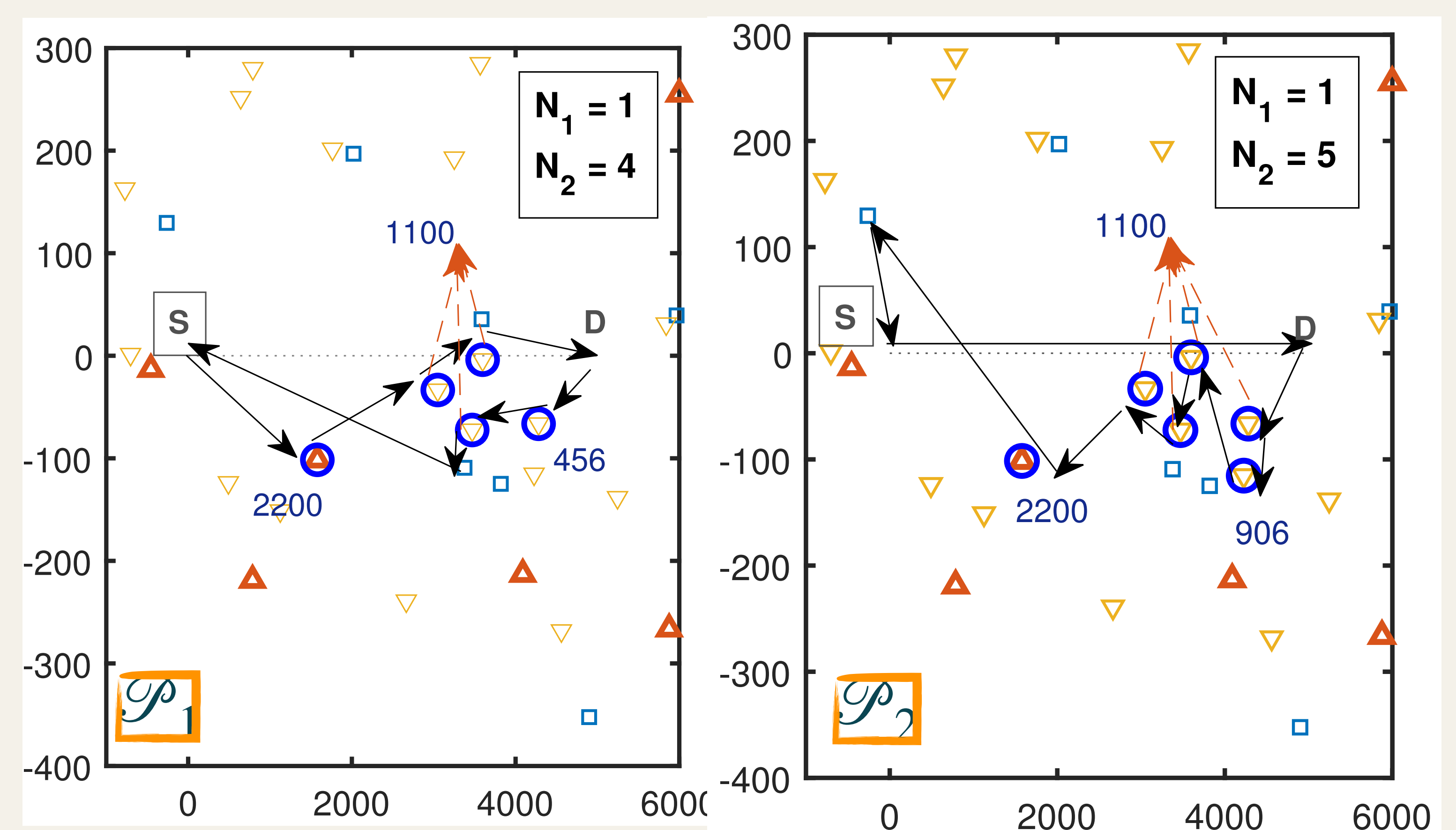
where  $T_{total}$  and  $M_{total}$  are the time and transmitted data of the trajectory,  $E_{total}$  and  $B_{max}$  are consumed energy and maximum onboard energy of UAVs.

## Data Delivery Efficiency

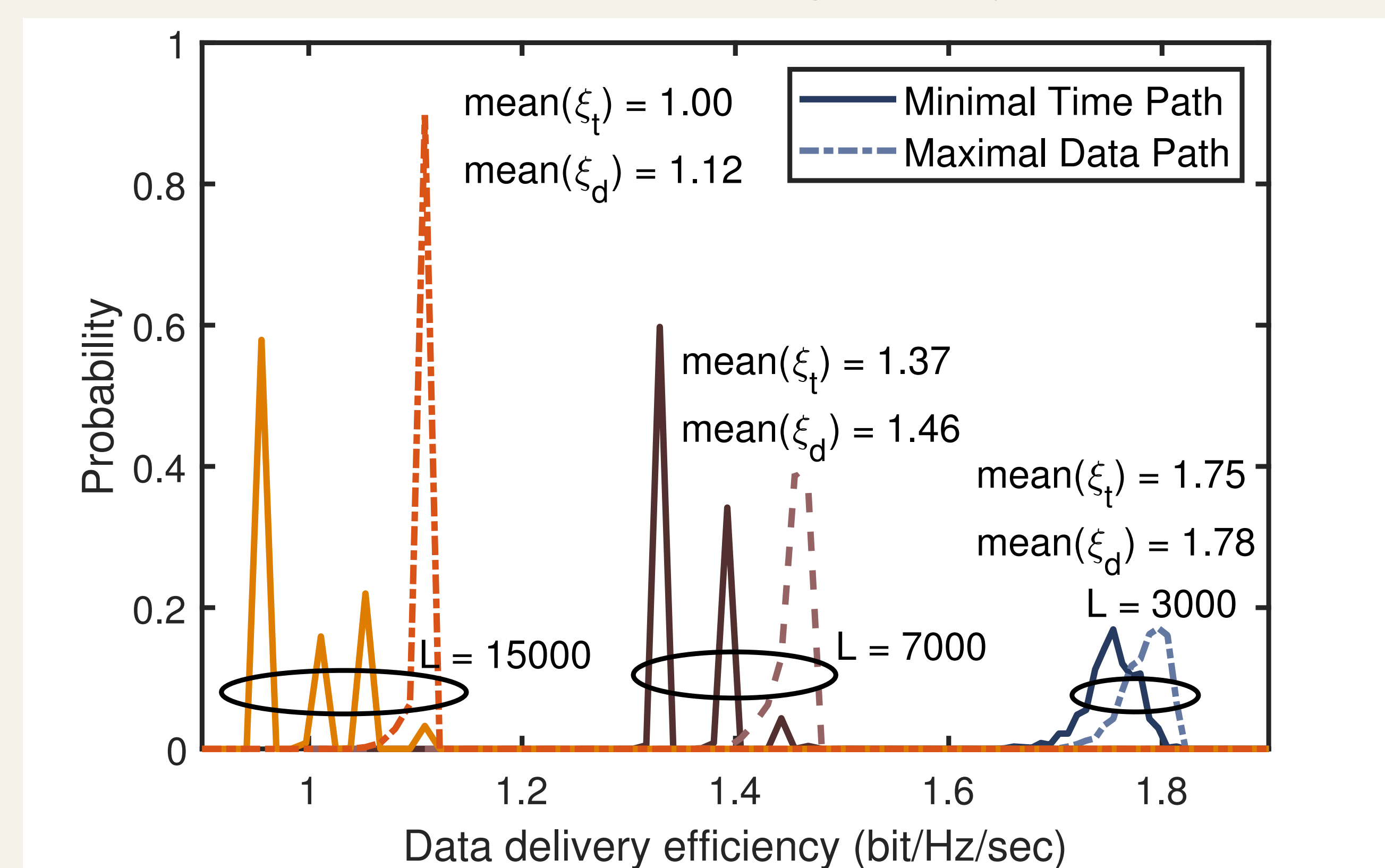
- Data delivery efficiency:

$$\xi = \mathbb{E}_{\Phi_{i,1}, \Phi_{i,2}, \Phi_b} \left[ \frac{M_{total}^* | \Phi_{i,1}, \Phi_{i,2}, \Phi_b}{T_{total}^* | \Phi_{i,1}, \Phi_{i,2}, \Phi_b} \right],$$

## Numerical Results



- Realizations of the optimal trajectory of UAV.



- The maximal data path has high efficiency under different L.
- The values of  $\xi_t$  for the minimal time path have several peaks because of the velocity.
- Minimal time path is more practical if the IoT data is limited and UAVs can deliver all of them.